## Math 126: College Algebra Spring 2022

Practice Problems for Final Exam

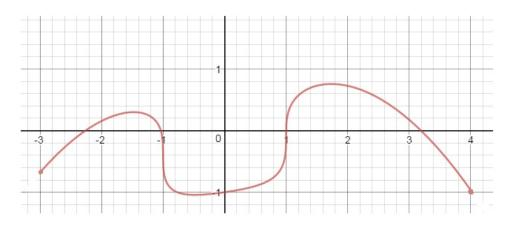
- 1. Simplify the expression  $\left(\frac{2x^3y^{-1}}{y^2}\right)^{-2}$  by eliminating any negative exponents.
- 2. Write the expression  $\frac{\sqrt[3]{8x^2}}{\sqrt{x}}$  using rational exponents and simplify.
- 3. Write the expression  $\frac{8}{\sqrt[3]{x^2}}$  with a rational denominator.
- 4. Find the product (x+3y)(2x-y) and simplify.
- 5. Find the product  $(x+2)(x^2+2x+3)$  and simplify.
- 6. Factor  $3x^3 x^2 12x + 4$  completely.
- 7. Factor  $8x^2 + 10x + 3$  completely.
- 8. Factor  $6x^2 5x 6$  completely.
- 9. Compute  $\frac{x^2+x-6}{x^2+4x-12} \div \frac{x+3}{x-1}$  and write your answer in lowest terms.
- 10. Compute  $\frac{4x}{x+2} \frac{2+3x}{x+2}$  and write your answer in lowest terms.
- 11. Compute  $\frac{2x}{x^2-16}-\frac{3}{x^2+8x+16}$  and write your answer in lowest terms.
- 12. Solve the equation 6 4x = 10.

- 13. Find the distance between the points (6, -2) and (-4, 5).
- 14. Find the midpoint of the segment that joins the points (5, -1) and (3, 5).
- 15. Find an equation of the circle of radius 5 centered at (-2,3).
- 16. Find the center and radius of the circle with equation  $x^2 + (y-2)^2 = 36$ .
- 17. Find the center and radius of the circle with equation  $x^2 + y^2 + 6y + 2 = 0$ .
- 18. Find an equation of the line with slope 7 that passes through (4, -1).
- 19. Find an equation of the line that passes through (6,2) and (-4,3).
- 20. Find an equation of the line that passes through (3,-1) that is parallel to y=6x+1.
- 21. Find an equation of the line that passes through (1,1) that is perpendicular to 2x + y = 4.
- 22. Find all real and complex solutions to  $x^2 + 14x = 32$ .
- 23. Find all real and complex solutions to  $2x^2 + 6x 5 = 0$ .
- 24. Find all real and complex solutions to  $3x^2 2x + 1 = 0$ .

- 25. Find all real solutions to  $\frac{6}{x^2-1}-\frac{3}{2}=\frac{3}{x-1}$ .
- 26. Find all real solutions to  $\frac{2}{x+3} + \frac{3}{8} = \frac{5}{4x+12}$ .
- 27. Find all real solutions to  $x^6 2x^3 3 = 0$ .
- 28. Find all real solutions to  $x^{3/2} 10x^{1/2} + 25x^{-1/2} = 0$ .
- 29. Find all real solutions to  $x^2\sqrt{x+3} = (x+3)^{3/2}$ .
- 30. Find all real solutions to  $x^5 x^3 2x = 0$ .
- 31. Solve the inequality 2 5x < 7.
- 32. Solve the inequality  $-4 < 2x 4 \le -2$ .
- 33. Solve the equation |8 3x| = 1.
- 34. Solve the inequality  $|4x+1| \ge 21$ .
- 35. Solve the inequality  $x^2 + 5x + 6 > 0$ .
- 36. Solve the inequality  $2x^2 + x \ge 1$ .

- 37. Consider the function  $f(x) = x^2 4x$ . Evaluate f(x-3) and simplify.
- 38. Find the domain of the function  $f(x) = \sqrt{4 x^2}$ .
- 39. Find the domain of the function  $f(x) = \frac{x-1}{x^2 + 3x 10}$
- 40. Find the domain of the function  $f(x) = \frac{5x}{\sqrt{x-1}}$ .
- 41. Find the average rate of change of the function  $f(x) = 6x x^2$  from x = 1 to x = 4.
- 42. If  $f(x) = 3\sqrt{x-4}$  and  $g(x) = x^2 1$ , find the formula for  $(f \circ g)(x)$ .
- 43. If  $f(x) = 3\sqrt{x-4}$  and  $g(x) = x^2 1$ , find the formula for  $(g \circ f)(x)$ .
- 44. If  $f(x) = 13x^{5/3} 1$ , find the formula for  $f^{-1}(x)$ .
- 45. If  $f(x) = \frac{2x+1}{3x-7}$ , find the formula for  $f^{-1}(x)$ .
- 46. Sketch a graph of the function  $f(x) = (x+1)^2 3$ .
- 47. Sketch a graph of the function f(x) = 3|x-1| + 2.
- 48. Sketch a graph of the function  $f(x) = \frac{1}{3}\sqrt{x+2}$ .

Consider the following graph of a function, y = f(x).



- 49. Find the domain of f.
- 50. Find, approximately, the range of f.
- 51. Find, approximately, the intervals where f is increasing.
- 52. Find, approximately, the intervals where f is decreasing.
- 53. Find, approximately, the intervals on which f(x) > 0.
- 54. Find the approximate coordinates of any local maxima of f.
- 55. Find the approximate coordinates of any local minima of f.
- 56. Is f a one-to-one function?
- 57. Sketch the graph of y = f(2 x) + 1.

- 58. Solve the inequality  $(x-2)^2(x+1)(x+3) < 0$ .
- 59. Solve the inequality  $\frac{x^2 9}{x^3 + x^2 4x 4} > 0$ .
- 60. Write the standard form of the quadratic function  $f(x) = 2x^2 8x + 4$ .
- 61. Find the coordinates of the vertex of the graph of  $y = x^2 5x + 2$ .
- 62. Find the maximum or minimum value of  $f(x) = 3x^2 8x + 4$ .
- 63. Determine the end behavior of the function  $f(x) = 3x^4 4x^3 10x 1$ .
- 64. Consider the function  $f(x) = x^4 + x^3 2x^2$ . Find all real zeros of f, state their multiplicities, and sketch the graph of f.
- 65. Consider the function  $f(x) = x x^3$ . Final all real zeros of f and their multiplicities, determine the end behavior of f, and sketch the graph of f.
- 66. Find the quotient and remainder of the division  $\frac{x^4 2x^2 + 7x}{x^2 x + 3}$ .
- 67. Find the quotient and remainder of the division  $\frac{x^2 5x + 4}{x 3}$ .
- 68. Let  $f(x) = x^5 2x^4 9x^3 + 22x^2 + 4x 24$ . Suppose that you know that 2 is a zero of f of multiplicity 3. Use this information to completely factor f.
- 69. Find a polynomial of degree 3 with integer coefficients and zeros at  $\frac{1}{2}$ , -1, and 2.
- 70. Let  $f(x) = \frac{1}{(x+2)^2}$ . Find all zeros of f, vertical asymptotes of f, and horizontal asymptotes of f. Find the behavior of the graph near the vertical asymptotes, and use this to sketch a graph of f.
- 71. Let  $f(x) = \frac{x^2 1}{x^2 2x 8}$ . Find all zeros of f, vertical asymptotes of f, and horizontal asymptotes of f. Find the behavior of the graph near the vertical asymptotes, and use this to sketch a graph of f.

- 72. Let  $f(x) = 4e^{4-x}$ . Use a calculator to find f(-1), rounded to three decimal places.
- 73. Write the equation  $\log_6(36) = 2$  in exponential form.
- 74. Write the equation  $4^x = 20$  in logarithmic form.
- 75. Let  $f(x) = 7\log_3(x+2)$ . Use the change of base formula and a calculator to find f(2), rounded to three decimal places.
- 76. Find the domain of the function  $f(x) = \ln(8-2x)$ .
- 77. Find the domain of the function  $f(x) = \frac{1}{\log_2(x)}$ .
- 78. Use the log laws to expand  $\log_3\left(\frac{(x+4)\sqrt{2x}}{(x+1)^7}\right)$ .
- 79. Write as a single logarithm using the log laws:  $\ln(4x) 2\ln(x-1) 6\ln(x+2)$ .
- 80. Sketch the graph of  $f(x) = 3^x 4$ .
- 81. Sketch the graph of  $f(x) = \log_2(x+3)$ .
- 82. Solve the equation  $3^{x-4} = 27$ .
- 83. Solve the equation  $e^{4x} + 4 = 9$ .
- 84. Solve the equation  $2^{2x} 2^x 12 = 0$ .

- 85. Solve the equation  $4^{5x-3} = 3^{4x-5}$ .
- 86. Solve the equation  $\log_{10}(2x-3) + 1 = 0$ .
- 87. Solve the equation  $\log_3(x^2 4) + \log_3(x) = \log_3(x 2)$ .
- 88. Solve the equation  $\log_8(x+5) \log_8(x-2) = 1$ .
- 89. You invest \$500 into an account with an annual interest rate of 8% that compounds monthly. How much money will be in your account after 2 years?
- 90. You invest \$800 into an account with an annual interest rate of 10% that compounds continuously. How much money will be in your account after 3 years?
- 91. You and your friend are each investing \$1000 into bank accounts. Your account has an annual interest rate of 6% and compounds continuously. Your friend's account compounds monthly, but you don't know the interest rate. At the end of 1 year, you end up with the exact same amount of money in your account as your friend has in her account. Find the annual interest rate of your friend's account.
- 92. Solve the system of equations

$$\begin{cases} x - 2y = 7 \\ 2x + 3y = -5 \end{cases}$$

93. Solve the system of equations

$$\begin{cases} x - 3y + z = -1 \\ 2x + 2y - 3z = 14 \\ 2z = -8 \end{cases}$$

94. Solve the system of equations

$$\begin{cases} x^2 - 2y = 6\\ 2x^2 + 8y^2 = 32 \end{cases}$$