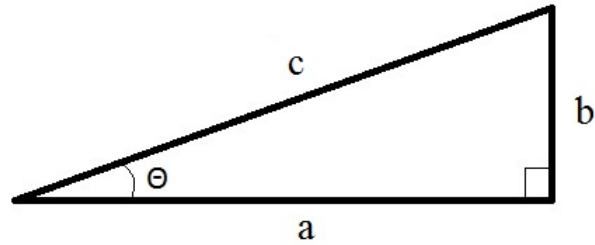


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1. Convert the angle 160° to radians.
 2. Convert the angle $\frac{\pi}{18}$ to degrees.
 3. Find an angle between 0 and 2π that is coterminal to $-\frac{19\pi}{7}$.
 4. Find the reference angle of $-\frac{19\pi}{7}$.
 5. If θ is an angle such that $\sin \theta < 0$ and $\tan \theta > 0$, in what quadrant must θ lie?
 6. A circle with a radius 4 has a sector with central angle 30° . Find the area of this sector.
 7. A circle with radius 3 has a sector with area 6π . Find the length of the arc surrounding this sector.
 8. What is the domain of the function $f(x) = \sin^{-1}(x)$?
 9. What is the range of the function $f(x) = \cos^{-1}(x)$?
 10. What is the range of the function $f(x) = \tan^{-1}(x)$?
 11. What is the amplitude of the function $f(x) = 3 \cos(7x - 2) + 5$?
 12. What is the period of the function $f(x) = 3 \cos(7x - 2) + 5$?

The following questions are based on a triangle of this form:



13. If $b = 3$ and $c = 4$, find a .

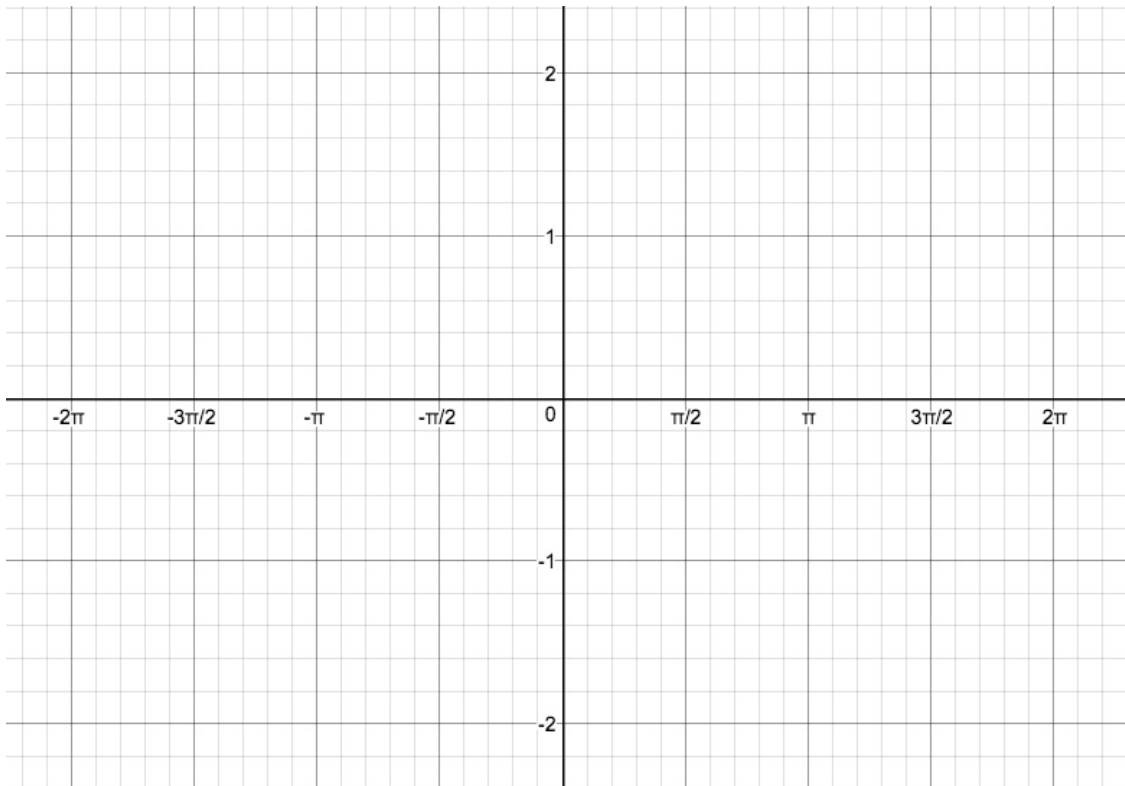
14. If $a = 5$ and $c = 7$, find $\tan \theta$.

15. If $a = 4$ and $\theta = 45^\circ$, find c .

16. If $b = 1$ and $c = 2$, find the value of θ .

17. If $b = 1$ and $c = 3$, find the area of the triangle.

24. On the grid below, sketch the graphs of $f(x) = 2\sin(3x)$ and $g(x) = \frac{1}{2}\cos(2x)$.



25. Review what the graphs of $\tan(x)$, $\cot(x)$, $\sec(x)$, and $\csc(x)$ look like. (For example, redo the graph-matching problem from Exam 1.)

26. Consider each of the following angles, expressed with inverse trig functions. Determine the quadrant of each angle.

(a) $\sin^{-1}\left(-\frac{2}{3}\right)$

(b) $\tan^{-1}\left(-\frac{2}{3}\right)$

(c) $\cos^{-1}\left(-\frac{2}{3}\right)$

27. For each of the following, find the exact value of the expression (that is, a rounded answer from your calculator will NOT be good enough).
- (a) $\sin^{-1}(\sin(\frac{2\pi}{3}))$

 - (b) $\tan(\tan^{-1}(-4))$

 - (c) $\csc(\sin^{-1}(0))$

 - (d) $\sin(\tan^{-1}(-1))$
28. Verify the identity $(1 - \tan x)(1 - \cot x) = 2 - \sec x \csc x$.
29. Verify the identity $\frac{\sin 2x}{\sin x} - \frac{\cos 2x}{\cos x} = \sec x$.
30. Verify the identity $(\cos x + \cos y)^2 + (\sin x - \sin y)^2 = 2 + 2 \cos(x + y)$.
31. Use a half-angle formula to find the exact value of $\tan 15^\circ$. (A rounded answer from your calculator will NOT be good enough.)
32. Use a half-angle formula to find the exact value of $\cos \frac{\pi}{8}$. (A rounded answer from your calculator will NOT be good enough.)
33. Write the expression $\csc(\tan^{-1} x)$ as an algebraic expression in terms of x .
34. Write the expression $\tan(\cos^{-1} x)$ as an algebraic expression in terms of x .
35. Write the expression $\cos(\sin^{-1} x + \cos^{-1} y)$ as an algebraic expression in terms of x and y .
36. Write the expression $\sin(2 \tan^{-1} x)$ as an algebraic expression in terms of x .

37. Solve the equation $4 \cos \theta = 1$.
38. Solve the equation $\cos \theta \sin \theta - \cos \theta = 0$.
39. Solve the equation $\sin \theta = \cos 2\theta$.
40. Let $z = 1 + i$, let $w = 1 - \sqrt{3}i$.
- Write z and w in polar form.
 - Compute zw .
 - Compute $(zw)^7$.
 - Compute $\frac{z^2}{w^3}$.
41. Consider the point $P = (-\sqrt{6}, \sqrt{2})$ in rectangular coordinates. Convert P to polar coordinates.
42. Consider the point $Q = (3, \pi/6)$ in polar coordinates. Convert Q to rectangular coordinates.
43. Using the variables x and y , convert the polar equation $r = 6 \sec \theta$ to rectangular coordinates.
44. Using the variables x and y , convert the polar equation $r = 2 \cos \theta$ to rectangular coordinates.
45. Using the variables x and y , convert the polar equation $r = 1 + \cos \theta$ to rectangular coordinates.

46. Consider the vector $\mathbf{v} = \langle 7, -2 \rangle$, and let \mathbf{u} be the vector with magnitude $\sqrt{8}$ and direction 135° .
- Write \mathbf{v} in terms of \mathbf{i} and \mathbf{j} .
 - Compute the magnitude of \mathbf{v} .
 - Compute the direction of \mathbf{v} .
 - Write \mathbf{u} in component form.
 - Compute the dot product $\mathbf{u} \cdot \mathbf{v}$.
 - Compute the angle between \mathbf{u} and \mathbf{v} .
 - Compute the vector $9\mathbf{u} + 4\mathbf{v}$ in component form.
 - Determine whether $9\mathbf{u} + 4\mathbf{v}$ is orthogonal to \mathbf{u} .
 - Calculate the component of \mathbf{u} along \mathbf{v} .
 - Calculate the projection of \mathbf{u} onto \mathbf{v} , $\text{proj}_{\mathbf{v}}\mathbf{u}$.
47. Write an equation for the parabola with vertex at the origin whose focus is the point $(0, -2)$.
48. Write an equation for an ellipse centered at the origin that has a focus at $(1, 0)$ and a vertex at $(3, 0)$.
49. Write an equation for a hyperbola centered at the origin that has a focus at $(0, 1)$ and asymptotes at $y = 2x$ and $y = -2x$.

50. Suppose a parabola has the equation $y^2 = 8x$. Find the focus and the directrix of this parabola.
51. Suppose an ellipse has the equation $4x^2 + 25y^2 = 100$. Find the foci of this ellipse and the length of its major axis.
52. Suppose a hyperbola has the equation $16x^2 - 4y^2 = 64$. Find the foci, vertices, and asymptotes of this hyperbola.
53. To estimate the height of a mountain above a level plain, the angle of elevation to the top of the mountain is measured to be 32° . One thousand feet closer to the mountain along the plain, it is found that the angle of elevation is 35° . Find the height of the mountain, to the nearest foot.
54. A 96-ft tree casts a shadow that is 120 ft long. What is the angle of elevation of the sun?
55. The Leaning Tower of Pisa leans 5.6° from the vertical. A tourist stands 105 m from its base with the tower leaning directly towards her. She measures the angle of elevation to the top of the tower to be 29.2° . Find the length of the tower, to the nearest meter.
56. A pilot heads his jet due east. The jet has a speed of 425 miles per hour relative to the air. The wind is blowing due north with a speed of 40 miles per hour. Find the true velocity of the jet as a vector.
57. A lawn mower is pushed a distance of 200 ft along a horizontal path by a constant force of 50 lb. The handle of the lawn mower is at an angle of 30° from the horizontal. Find the work done.