Fall 2020

Practice Problems for Cumulative

Algebra Exam

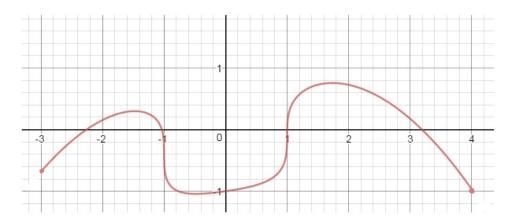
- 1. Simplify the expression $\left(\frac{2x^3y^{-1}}{y^2}\right)^{-2}$ by eliminating any negative exponents.
- 2. Write the expression $\frac{\sqrt[3]{8x^2}}{\sqrt{x}}$ using rational exponents and simplify.
- 3. Write the expression $\frac{8}{\sqrt[3]{x^2}}$ with a rational denominator.
- 4. Find the product (x+3y)(2x-y) and simplify.
- 5. Find the product $(x+2)(x^2+2x+3)$ and simplify.
- 6. Factor $3x^3 x^2 12x + 4$ completely.
- 7. Factor $8x^2 + 10x + 3$ completely.
- 8. Factor $6x^2 5x 6$ completely.
- 9. Compute $\frac{x^2+x-6}{x^2+4x-12} \div \frac{x+3}{x-1}$ and write your answer in lowest terms.
- 10. Compute $\frac{4x}{x+2} \frac{2+3x}{x+2}$ and write your answer in lowest terms.
- 11. Compute $\frac{2x}{x^2-16}-\frac{3}{x^2+8x+16}$ and write your answer in lowest terms.
- 12. Solve the equation 6 4x = 10.

- 13. Find the distance between the points (6, -2) and (-4, 5).
- 14. Find the midpoint of the segment that joins the points (5,-1) and (3,5).
- 15. Find an equation of the circle of radius 5 centered at (-2,3).
- 16. Find the center and radius of the circle with equation $x^2 + (y-2)^2 = 36$.
- 17. Find the center and radius of the circle with equation $x^2 + y^2 + 6y + 2 = 0$.
- 18. Find an equation of the line with slope 7 that passes through (4, -1).
- 19. Find an equation of the line that passes through (6,2) and (-4,3).
- 20. Find an equation of the line that passes through (3,-1) that is parallel to y=6x+1.
- 21. Find an equation of the line that passes through (1,1) that is perpendicular to 2x + y = 4.
- 22. Find all real and complex solutions to $x^2 + 14x = 32$.
- 23. Find all real and complex solutions to $2x^2 + 6x 5 = 0$.
- 24. Find all real and complex solutions to $3x^2 2x + 1 = 0$.

- 25. Find all real solutions to $\frac{6}{x^2-1}-\frac{3}{2}=\frac{3}{x-1}$.
- 26. Find all real solutions to $\frac{2}{x+3} + \frac{3}{8} = \frac{5}{4x+12}$.
- 27. Find all real solutions to $x^6 2x^3 3 = 0$.
- 28. Find all real solutions to $x^{3/2} 10x^{1/2} + 25x^{-1/2} = 0$.
- 29. Find all real solutions to $x^2\sqrt{x+3} = (x+3)^{3/2}$.
- 30. Find all real solutions to $x^5 x^3 2x = 0$.
- 31. Solve the inequality 2 5x < 7.
- 32. Solve the inequality $-4 < 2x 4 \le -2$.
- 33. Solve the equation |8 3x| = 1.
- 34. Solve the inequality $|4x + 1| \ge 21$.
- 35. Solve the inequality $x^2 + 5x + 6 > 0$.
- 36. Solve the inequality $2x^2 + x \ge 1$.

- 37. Consider the function $f(x) = x^2 4x$. Evaluate f(x-3) and simplify.
- 38. Find the domain of the function $f(x) = \sqrt{4 x^2}$.
- 39. Find the domain of the function $f(x) = \frac{x-1}{x^2 + 3x 10}$
- 40. Find the domain of the function $f(x) = \frac{5x}{\sqrt{x-1}}$.
- 41. Find the average rate of change of the function $f(x) = 6x x^2$ from x = 1 to x = 4.
- 42. If $f(x) = 3\sqrt{x-4}$ and $g(x) = x^2 1$, find the formula for $(f \circ g)(x)$.
- 43. If $f(x) = 3\sqrt{x-4}$ and $g(x) = x^2 1$, find the formula for $(g \circ f)(x)$.
- 44. If $f(x) = 13x^{5/3} 1$, find the formula for $f^{-1}(x)$.
- 45. If $f(x) = \frac{2x+1}{3x-7}$, find the formula for $f^{-1}(x)$.
- 46. Sketch a graph of the function $f(x) = \sqrt[3]{x^2 1}$ by making a table of values and plotting some points.

Consider the following graph of a function, y = f(x).



- 47. Find the domain of f.
- 48. Find, approximately, the range of f.
- 49. Find, approximately, the intervals where f is increasing.
- 50. Find, approximately, the intervals where f is decreasing.
- 51. Find, approximately, the intervals on which f(x) > 0.
- 52. Find the approximate coordinates of any local maxima of f.
- 53. Find the approximate coordinates of any local minima of f.
- 54. Is f a one-to-one function?
- 55. Sketch the graph of y = f(2 x) + 1.

- 56. Solve the inequality $\frac{x^2 9}{x^3 + x^2 4x 4} > 0$.
- 57. Write the standard form of the quadratic function $f(x) = 2x^2 8x + 4$.
- 58. Find the coordinates of the vertex of the graph of $y = x^2 5x + 2$.
- 59. Find the maximum or minimum value of $f(x) = 3x^2 8x + 4$.
- 60. Determine the end behavior of the function $f(x) = 3x^4 4x^3 10x 1$.
- 61. Consider the function $f(x) = x^4 + x^3 2x^2$. Find all real zeros of f, state their multiplicities, and sketch the graph of f.
- 62. Consider the function $f(x) = x x^3$. Final all real zeros of f and their multiplicities, determine the end behavior of f, and sketch the graph of f.
- 63. Find the quotient and remainder of the division $\frac{x^4 2x^2 + 7x}{x^2 x + 3}$.
- 64. Find the quotient and remainder of the division $\frac{x^2 5x + 4}{x 3}$.
- 65. Let $f(x) = x^5 2x^4 9x^3 + 22x^2 + 4x 24$. Suppose that you know that 2 is a zero of f of multiplicity 3. Use this information to completely factor f.
- 66. Find a polynomial of degree 3 with integer coefficients and zeros at $\frac{1}{2}$, -1, and 2.

- 67. Let $f(x) = 4e^{4-x}$. Use a calculator to find f(-1), rounded to three decimal places.
- 68. Write the equation $\log_6(36) = 2$ in exponential form.
- 69. Write the equation $4^x = 20$ in logarithmic form.
- 70. Let $f(x) = 7\log_3(x+2)$. Use the change of base formula and a calculator to find f(2), rounded to three decimal places.
- 71. Find the domain of the function $f(x) = \ln(8-2x)$.
- 72. Find the domain of the function $f(x) = \frac{1}{\log_2(x)}$.
- 73. Use the log laws to expand $\log_3\left(\frac{(x+4)\sqrt{2x}}{(x+1)^7}\right)$.
- 74. Write as a single logarithm using the log laws: $\ln(4x) 2\ln(x-1) 6\ln(x+2)$.
- 75. Solve the equation $3^{x-4} = 27$.
- 76. Solve the equation $e^{4x} + 4 = 9$.
- 77. Solve the equation $2^{2x} 2^x 12 = 0$.

- 78. Solve the equation $4^{5x-3} = 3^{4x-5}$.
- 79. Solve the equation $\log_{10}(2x-3) + 1 = 0$.
- 80. Solve the equation $\log_3(x^2 4) + \log_3(x) = \log_3(x 2)$.
- 81. Solve the equation $\log_8(x+5) \log_8(x-2) = 1$.
- 82. You invest \$500 into an account with an annual interest rate of 8% that compounds monthly. How much money will be in your account after 2 years?
- 83. You invest \$800 into an account with an annual interest rate of 10% that compounds continuously. How much money will be in your account after 3 years?
- 84. You and your friend are each investing \$1000 into bank accounts. Your account has an annual interest rate of 6% and compounds continuously. Your friend's account compounds monthly, but you don't know the interest rate. At the end of 1 year, you end up with the exact same amount of money in your account as your friend has in her account. Find the annual interest rate of your friend's account.