1. Convert the angle $160°$ to radians.

2. Convert the angle $\frac{\pi}{18}$ to degrees.

3. Find an angle between 0 and 2π that is coterminal to $-\frac{19\pi}{7}$.

4. Find the reference angle of $-\frac{19\pi}{7}$.

5. If θ is an angle such that $\sin(\theta) < 0$ and $\tan(\theta) > 0$, in what quadrant must θ lie?

6. Find the terminal point on the unit circle determined by $t = \dfrac{\pi}{6}$.

7. A circle with radius 3 has a sector with area 6π. Find the length of the arc surrounding this sector.

8. What is the domain of the function $f(x) = \sin^{-1}(x)$?

9. What is the range of the function $f(x) = \cos^{-1}(x)$?

10. What is the range of the function $f(x) = \tan^{-1}(x)$?

11. What is the amplitude of the function $f(x) = 3\cos(7x - 2) + 5$?

12. What is the period of the function $f(x) = 3\cos(7x - 2) + 5$?

The following questions are based on a triangle of this form:
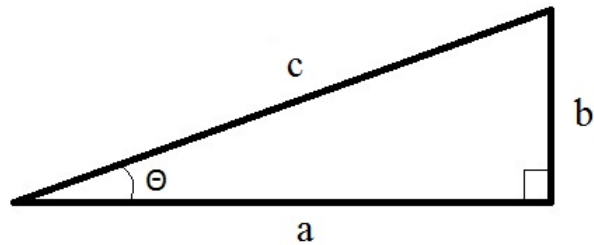
13. If $b = 3$ and $c = 4$, find a.

14. If $a = 5$ and $c = 7$, find $\tan \theta$.

15. If $a = 4$ and $\theta = 45°$, find c.

16. If $b = 1$ and $c = 2$, find the value of θ.

17. If $b = 1$ and $c = 3$, find the area of the triangle.

In these problems, you are given three parts of an oblique triangle, where side a is opposite angle A, side b is opposite angle B, and side c is opposite angle C. In each problem, follow the instructions to give the desired information.

18. Suppose that $A = 30°$, $C = 80°$, and $b = 10$. Find the length of side a.

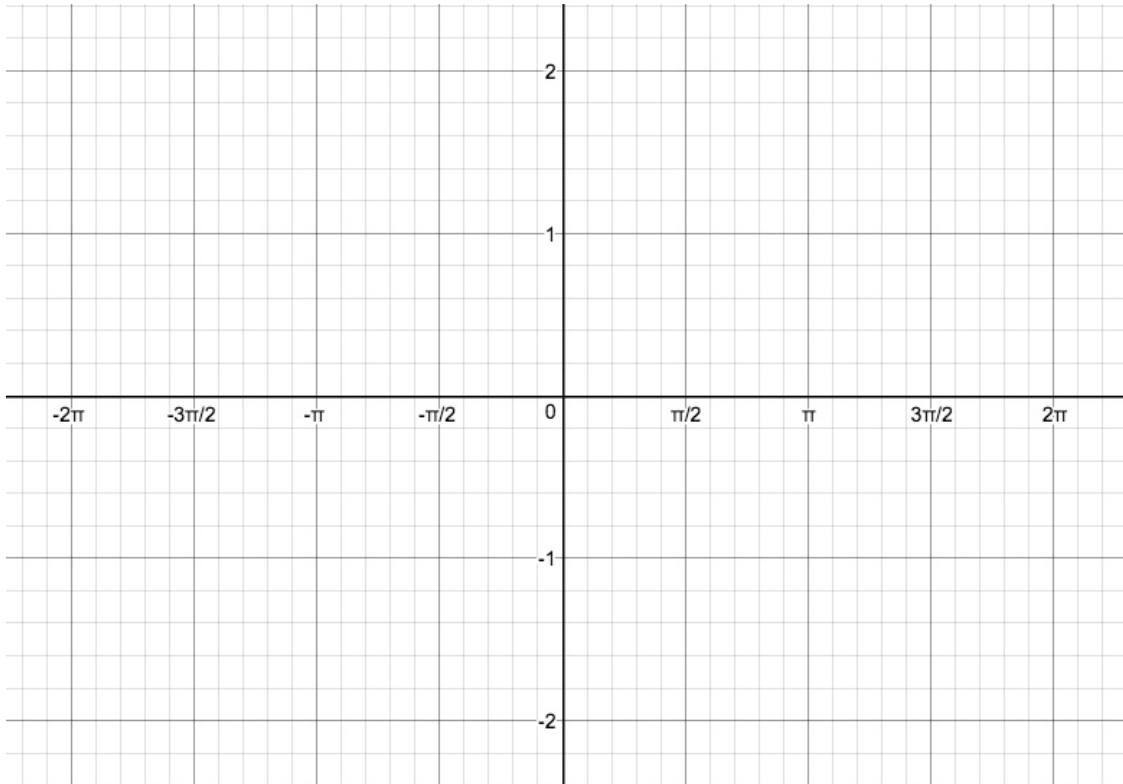19. Suppose that $A = 40°$, $B = 70°$, and $a = 2$. Find the length of side b.

20. Suppose that $a = 8$, $b = 10$, and $c = 12$. Find the measure of angle A.

21. Suppose that $A = 120°$, $b = 8$, $c = 2$. Find the length of side a.

22. Suppose that $A = 35°$, $b = 2$, $c = 7$. Find the area of the triangle.

23. Suppose that $A = 25°$, $a = 12$, and $c = 23$. How many possible solutions are there to this triangle?

24. On the grid below, sketch the graphs of $f(x) = 2\sin(x)$ and $g(x) = \cos(x) - 1$.

25. Review what the graphs of $\tan(x)$, $\cot(x)$, $\sec(x)$, and $\csc(x)$ look like. (For example, redo the graph-matching problem from Exam 3.)

26. Consider each of the following angles, expressed with inverse trig functions. Determine the quadrant of each angle.
    (a) $\sin^{-1}\left(-\frac{2}{3}\right)$

    (b) $\tan^{-1}\left(-\frac{2}{3}\right)$

    (c) $\cos^{-1}\left(-\frac{2}{3}\right)$

27. For each of the following, find the exact value of the expression (that is, a rounded answer from your calculator will NOT be good enough).
    (a) $\sin^{-1}(\sin(\frac{2\pi}{3}))$

    (b) $\tan(\tan^{-1}(-4))$

    (c) $\csc(\sin^{-1}(0))$

    (d) $\sin(\tan^{-1}(-1))$

28. Verify the identity $(1 - \tan x)(1 - \cot x) = 2 - \sec x \csc x$.

29. Verify the identity $\dfrac{\sin 2x}{\sin x} - \dfrac{\cos 2x}{\cos x} = \sec x$.

30. Verify the identity $(\cos x + \cos y)^2 + (\sin x - \sin y)^2 = 2 + 2\cos(x + y)$.

31. Use a half-angle formula to find the exact value of $\tan(15°)$. (A rounded answer from your calculator will NOT be good enough.)

32. Use a half-angle formula to find the exact value of $\sin\left(\dfrac{\pi}{8}\right)$. (A rounded answer from your calculator will NOT be good enough.)

33. Write the expression $\csc(\tan^{-1} x)$ as an algebraic expression in terms of x.

34. Write the expression $\tan(\cos^{-1} x)$ as an algebraic expression in terms of x.

35. Write the expression $\cos(\sin^{-1} x + \cos^{-1} y)$ as an algebraic expression in terms of x and y.

36. Write the expression $\sin(2\tan^{-1} x)$ as an algebraic expression in terms of x.

37. Solve the equation $4\cos\theta = 1$.

38. Solve the equation $\cos\theta\sin\theta - \cos\theta = 0$.

39. Solve the equation $\tan(3\theta) = 5$

40. Solve the equation $\sin\theta = \cos 2\theta$.

41. Let $z = 1 + i$, let $w = 1 - \sqrt{3}i$.
    (a) Write z and w in polar form.

    (b) Compute zw.

    (c) Compute $(zw)^7$.

    (d) Compute $\frac{z^2}{w^3}$.

42. Consider the point $P = (-\sqrt{6}, \sqrt{2})$ in rectangular coordinates. Convert P to polar coordinates.

43. Consider the point $Q = (3, \pi/6)$ in polar coordinates. Convert Q to rectangular coordinates.

44. Using the variables x and y, convert the polar equation $r = 6\sec\theta$ to rectangular coordinates.

45. Using the variables x and y, convert the polar equation $r = 2\cos\theta$ to rectangular coordinates.

46. Using the variables x and y, convert the polar equation $r = 1+\cos\theta$ to rectangular coordinates.

47. Consider the vector $\mathbf{v} = \langle 7, -2 \rangle$, and let $\mathbf{u}$ be the vector with magnitude $\sqrt{8}$ and direction $135°$.

    (a) Write $\mathbf{v}$ in terms of $\mathbf{i}$ and $\mathbf{j}$.

    (b) Compute the magnitude of $\mathbf{v}$.

    (c) Compute the direction of $\mathbf{v}$.

    (d) Write $\mathbf{u}$ in component form.

    (e) Compute the dot product $\mathbf{u} \cdot \mathbf{v}$.

    (f) Compute the angle between $\mathbf{u}$ and $\mathbf{v}$.

    (g) Compute the vector $9\mathbf{u} + 4\mathbf{v}$ in component form.

    (h) Determine whether $9\mathbf{u} + 4\mathbf{v}$ is orthogonal to $\mathbf{u}$.

    (i) Calculate the component of $\mathbf{u}$ along $\mathbf{v}$.

    (j) Calculate the projection of $\mathbf{u}$ onto $\mathbf{v}$, $\text{proj}_{\mathbf{v}}\mathbf{u}$.

48. To estimate the height of a mountain above a level plain, the angle of elevation to the top of the mountain is measured to be $32°$. One thousand feet closer to the mountain along the plain, it is found that the angle of elevation is $35°$. Find the height of the mountain, to the nearest foot.

49. A 96-ft tree casts a shadow that is 120 ft long. What is the angle of elevation of the sun?

50. The Leaning Tower of Pisa leans $5.6°$ from the vertical. A tourist stands 105 m from its base with the tower leaning directly towards her. She measures the angle of elevation to the top of the tower to be $29.2°$. Find the length of the tower, to the nearest meter.

51. A lawn mower is pushed a distance of 200 ft along a horizontal path by a constant force of 50 lb. The handle of the lawn mower is at an angle of $30°$ from the horizontal. Find the work done.