## Homework 2, due Tuesday, February 1

Please turn in solutions for the following problems:

(1) Sketch each set and determine if each set is open, closed, connected, or bounded:

(a)  $|2z - 4 + 6i| \le 4$ 

(b) 1 < |z| < 2

(d)  $0 \le \arg(z) \le \pi/4$ (e)  $(\text{Re}(z))^2 + 1 = (\text{Im}(z))^2$ 

(c)  $\operatorname{Re}(z) > \operatorname{Im}(z)$ 

(2) For each of the following functions, determine the largest possible domain of definition.

(a)  $f(z) = \frac{1}{z^2 + 1}$ 

(b)  $f(z) = \frac{z}{z - \overline{z}}$ 

(c)  $f(z) = \frac{1}{1 - |z|^2}$ 

(d)  $f(z) = \operatorname{Arg}\left(\frac{1}{z}\right)$ 

- (3) Consider the function f(z) = Arg(z), and let S be the horizontal line  $\operatorname{Im}(z) = 1$ . Sketch the image set f(S).
- (4) Let  $f(z) = e^z$ . Compute each value. (Round to an appropriate number of decimal places if needed).

(a)  $f(-1+i\pi)$ 

(b)  $f(\pi/2)$ 

- (5) Consider the function  $f(z) = e^z$ , and let S be the vertical line Re(z) = 1. Sketch the image set f(S).
- (6) Let f(z) = Log(z). Compute each value. (Write in terms of  $\pi$  if possible, but otherwise, round to an appropriate number of decimal places if needed).

(a)  $f(\sqrt{3} - i)$ 

(b) f(-4+4i)

(7) Consider the function f(z) = Log(z), and let S be the right half-circle of radius 1 centered at 0. That is,  $S = \{z \in \mathbb{C} \mid |z| = 1 \text{ and } \operatorname{Re}(z) \geq 0\}.$ Sketch the image set f(S).

In addition, I suggest that you work these problems from the Brown/Churchill textbook (but do not turn in):

- Page 33, problems 1, 2, 3
- Page 44, problems 3, 4, 7
- Page 92, problems 1, 8
- Page 97, problems 1, 2, 7