

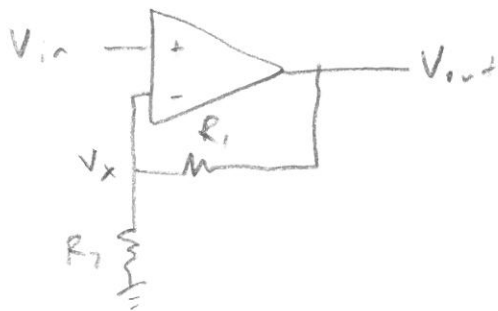
KCL

$$\frac{V_{in}}{R_1} + \frac{V_{out}}{R_2} = 0$$

$$\frac{V_{out}}{V_{in}} = -\frac{R_2}{R_1}$$

II  $R_1 = 10\text{k}\Omega$   
 $R_2 = 1\text{k}\Omega$

$$\frac{V_{out}}{V_{in}} = -\frac{1\text{k}\Omega}{10\text{k}\Omega} = -\frac{1}{10} = -0.1$$



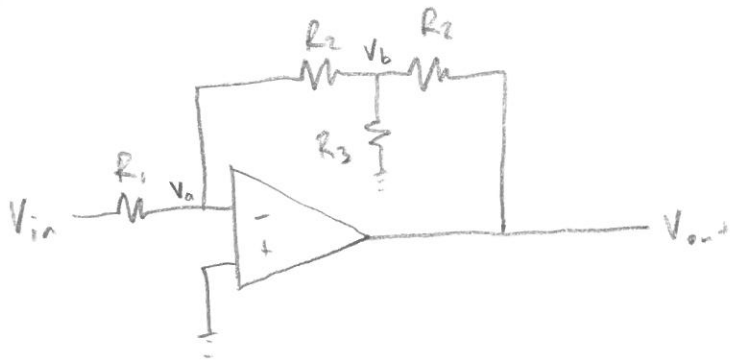
$$V_x = V_{out} \frac{R_2}{R_1 + R_2}$$

Negative Feedback  $\Rightarrow V_{in} = V_x$

$$\frac{V_{out}}{V_{in}} = \frac{R_1 + R_2}{R_2} = 1 + \frac{R_1}{R_2}$$

II  $R_1 = 10\text{k}\Omega$   
 $R_2 = 1\text{k}\Omega$

$$\frac{V_{out}}{V_{in}} = 1 + \frac{10\text{k}\Omega}{1\text{k}\Omega} = 11$$



Negative Feedback  $\Rightarrow V_a = 0$

$$V_b = V_{out} \frac{R_2 // R_3}{R_2 + R_2 // R_3}$$

KCL @  $V_a$

$$\frac{V_{in}}{R_1} + \frac{V_b}{R_2} = 0$$

$$\frac{V_b}{V_{in}} = -\frac{R_2}{R_1}$$

$$\frac{V_{out}}{V_{in}} \frac{R_2 // R_3}{R_2 + R_2 // R_3} = -\frac{R_2}{R_1}$$

$$\frac{V_{out}}{V_{in}} = -\frac{R_2}{R_1} \left( \frac{R_2 + R_2 // R_3}{R_2 // R_3} \right) = -\frac{R_2}{R_1} \left( 1 + \frac{R_2}{R_2 // R_3} \right)$$

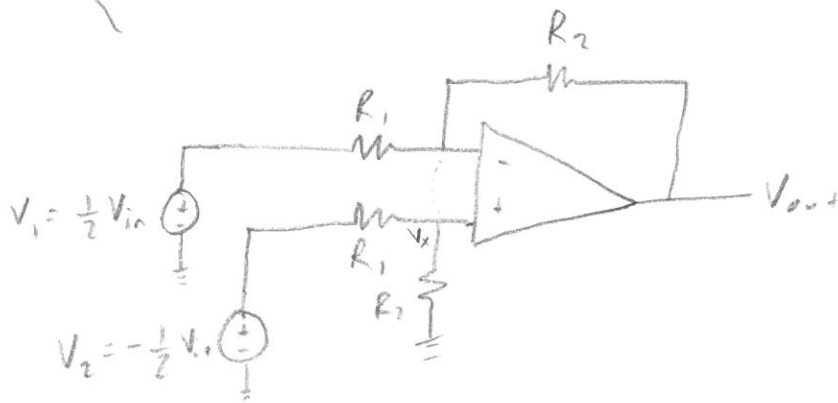
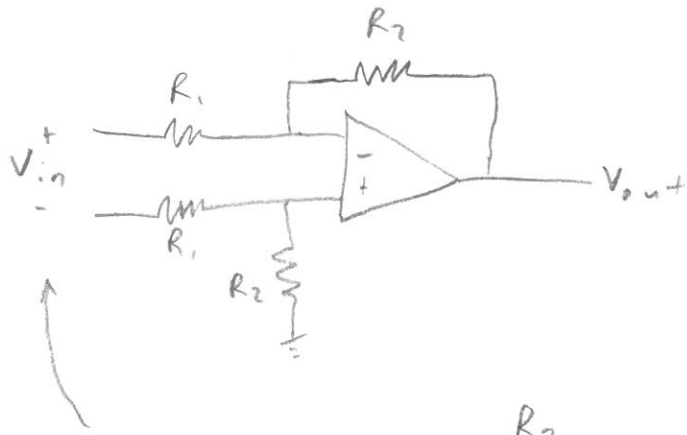
$$\frac{V_{out}}{V_{in}} = -\frac{R_2}{R_1} \left( 1 + \frac{R_2}{\frac{R_2 R_3}{R_2 + R_3}} \right) = -\frac{R_2}{R_1} \left( 1 + \frac{R_2 + R_3}{R_3} \right)$$

$$\frac{V_{out}}{V_{in}} = -\frac{R_2}{R_1} \left( 2 + \frac{R_2}{R_3} \right)$$

If  $R_1 = 1k\Omega$ ,  $R_2 = 10k\Omega$ ,  $R_3 = 100\Omega$

$$\frac{V_{out}}{V_{in}} = -1020$$

Note - This "T-configuration" provides more gain than a simple inverting amplifier for smaller total resistance values (assuming  $R_{in}$  is fixed)



$$V_x = V_2 \frac{R_2}{R_1 + R_2}$$

$$\text{KCL} \Rightarrow \frac{V_1 - V_x}{R_1} + \frac{V_{out} - V_x}{R_2} = 0$$

$$V_{out} = -\frac{R_2}{R_1} V_1 + \left(1 + \frac{R_2}{R_1}\right) V_x$$

$$V_{out} = -\frac{R_2}{R_1} V_1 + \frac{R_2}{R_1} V_2 = -\frac{R_2}{R_1} (V_1 - V_2)$$

$$V_1 - V_2 = \frac{1}{2} V_{in} - \left(-\frac{1}{2}\right) V_{in} = V_{in}$$

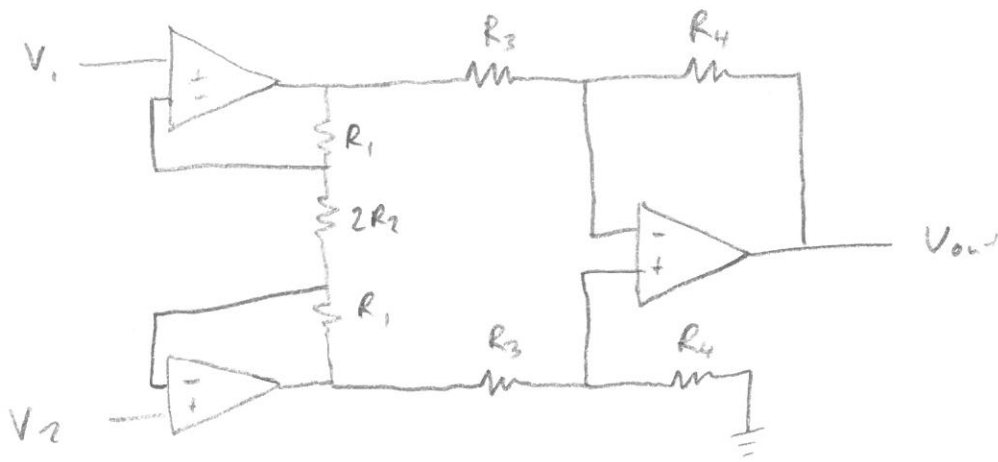
$$V_{out} = -\frac{R_2}{R_1} V_{in}$$

$$\frac{V_{out}}{V_{in}} = -\frac{R_2}{R_1}$$

$$\text{If } R_1 = 1 \text{ k}\Omega$$

$$R_2 = 10 \text{ k}\Omega$$

$$\frac{V_{out}}{V_{in}} = \frac{-10 \text{ k}\Omega}{1 \text{ k}\Omega} = -10$$



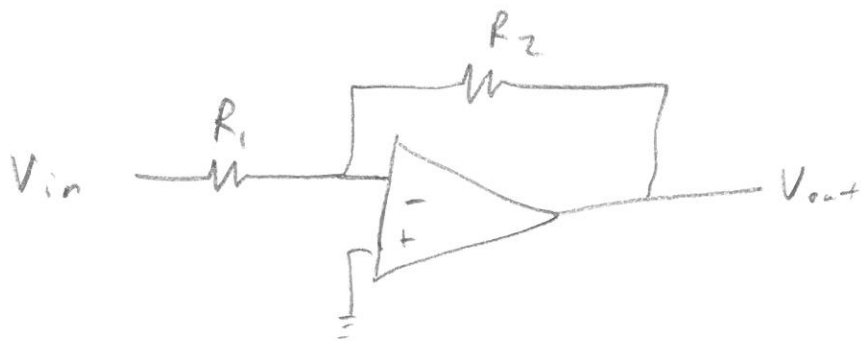
Instrumentation Amplifier

$$\frac{V_{out}}{V_1 - V_2} = \left( -\frac{R_4}{R_3} \right) \left( 1 + \frac{R_1}{R_2} \right)$$

If  $R_1 = 1k\Omega$ ,  $R_2 = 100\Omega$ ,  $R_3 = 100\Omega$ ,  $R_4 = 1k\Omega$

$$\frac{V_{out}}{V_1 - V_2} = 110$$

Design an amplifier with  $R_{in} = 50\Omega$  and  $|\text{Gain}| = 1000$   
The inverting amplifier permits setting a specific input impedance



$$\frac{V_{out}}{V_{in}} =$$

$$R_{in} = R_1$$

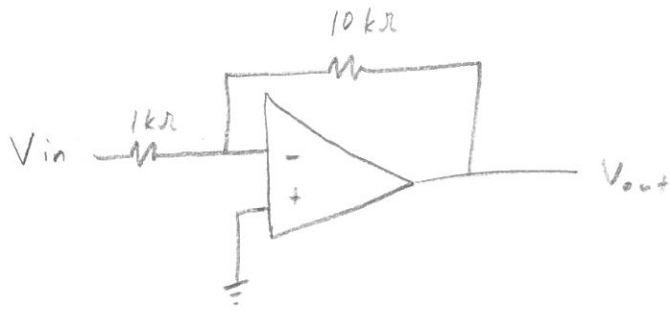
$$\text{Let } R_1 = 50\Omega$$

$$R_2 = -R_1 \left( \frac{V_{out}}{V_{in}} \right) = (-50\Omega) (-1000) = 50k\Omega$$

Summary

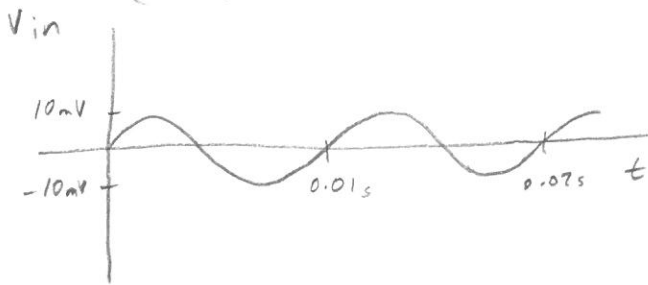
$$R_1 = 50\Omega$$

$$R_2 = 50k\Omega$$



$$\frac{V_{out}}{V_{in}} = \frac{-10k\Omega}{1k\Omega} = -10 \Rightarrow \text{Gain}$$

$$V_{in} = (10\text{mV}) \sin(2\pi(100\text{Hz})t)$$

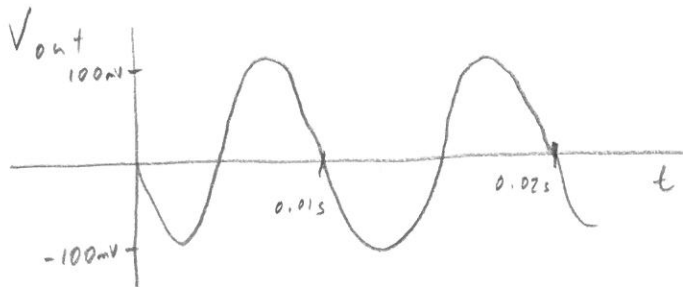


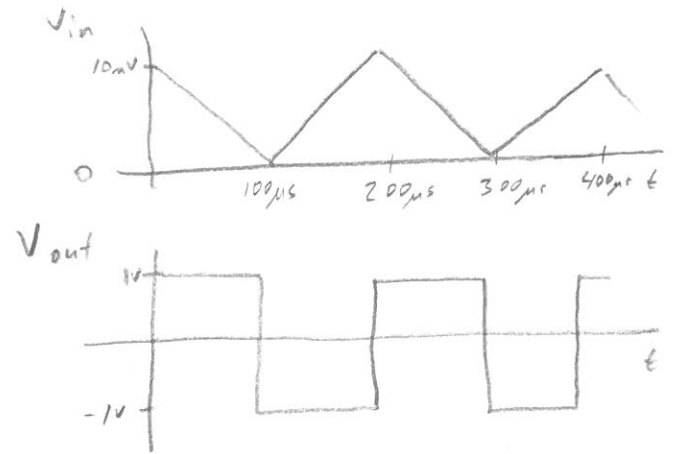
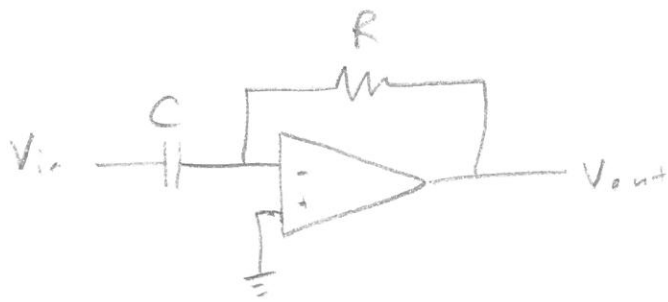
$$\omega = (2\pi)(100\text{Hz})$$

$$f = 100\text{Hz}$$

$$\frac{1}{f} = T = \frac{1}{100\text{Hz}} = 0.01\text{s}$$

↑ period of the input signal





Let  $C = 10\mu\text{F}$  Find  $R$

This is a differentiator circuit +

KCL

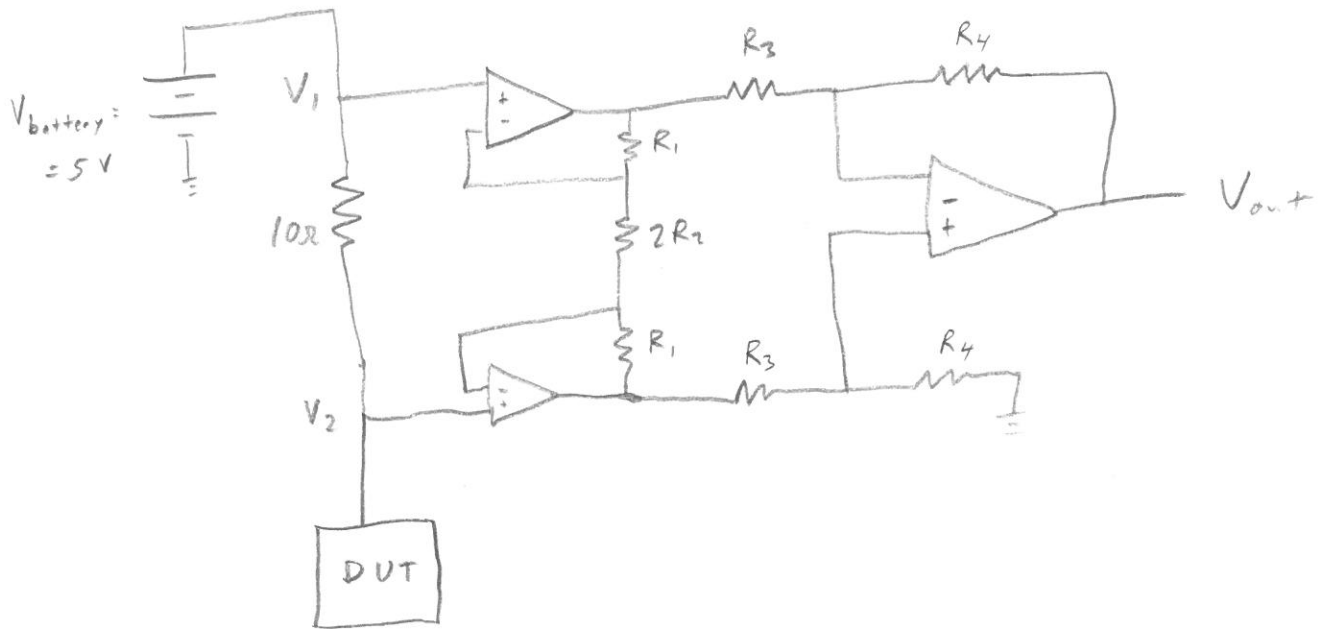
$$C \frac{dV_{in}}{dt} + \frac{V_{out}}{R} = 0$$

$$V_{out} = -RC \frac{dV_{in}}{dt}$$

This circuit finds the negative of the slope  
 $\text{slope} = \frac{\text{rise}}{\text{run}}$  and slope must equal  $\pm 1$

$$V_{out} = 1V = -RC \frac{-10\text{mV}}{100\mu\text{s}}$$

$$R = \frac{-1V}{C} \left( \frac{-100\mu\text{s}}{10\text{mV}} \right) = \boxed{1\text{k}\Omega}$$



Let  $R_1 = 100\text{k}\Omega$ ,  $R_2 = 100\Omega$ ,  $R_3 = 1\text{k}\Omega$ ,  $R_4 = 100\text{k}\Omega$

$V_{out} = -1\text{V}$

Determine how much current flows through the  $10\Omega$  resistor?

This is an instrumentation amplifier, so

$$V_{out} = -\left(\frac{R_4}{R_3}\right)\left(1 + \frac{R_1}{R_2}\right)(V_1 - V_2)$$

$V_1 - V_2$  is the voltage drop across the  $10\Omega$  resistor

$$V_1 - V_2 = \frac{V_{out}}{-\left(\frac{R_4}{R_3}\right)\left(1 + \frac{R_1}{R_2}\right)} = 9.99\mu\text{V}$$

$$V = IR$$

$$\therefore I = \frac{V_1 - V_2}{R} = \frac{9.99\mu\text{V}}{10\Omega} = \boxed{999\text{ nA}}$$