

FINAL EXAM MATERIAL AND EXPECTATIONS

For the final exam, you should be able to do the following things:

Chapter 2.

- Given a graph, find one-sided and two-sided limits
- Evaluate easy limits by plugging in the value
- Use limit laws to rewrite limits as necessary
- Evaluate harder limits by using some tricks, which include:
 - factoring polynomials and canceling common factors
 - expanding out polynomials, combining like terms, and refactoring
 - simplifying radicals by multiplying by the conjugate
 - simplifying complex fractions by rewriting as a single fraction
 - considering piecewise-defined functions by looking at left and right limits separately
 - rewriting absolute value as a piecewise-defined function
- Use the Squeeze Theorem to find limits
- Determine if a function is continuous using limits
- Determine whether a discontinuity is removable, jump, or infinite
- Use $\lim_{x \rightarrow 0} \frac{\sin(x)}{x}$ to compute limits

Chapter 3.

- Use the limit definition of the derivative to compute the derivative of a function at a point
- Use the basic differentiation rules, including:
 - derivative of a sum is the sum of the derivatives
 - derivative of a constant multiple is constant multiple of the derivative
 - product rule
 - quotient rule
 - chain rule
- Know the derivatives of powers of x and trig functions (full list of derivatives to know is at the end)
- Find the equation of a tangent line to a curve
- Use implicit differentiation to find $\frac{dy}{dx}$ for an implicitly defined curve
- Compute second derivatives, and general higher derivatives
- Use logarithmic differentiation to differentiate messy functions

Chapter 4.

- Solve related rates problems
- Use the linearization formula to estimate values of functions
- Use f' to get where f is increasing or decreasing and find local maxima and minima
- Use f'' to get where f is concave up or concave down and find inflection points
- Compute limits at infinity and negative infinity
- Use limit info to check for vertical and horizontal asymptotes
- Sketch the graph of a function using the previous ingredients
- Solve optimization problems

- Use l'Hôpital's Rule to evaluate limits of indeterminate forms, including

$-\frac{0}{0}$ form	$-\ 0 \cdot \infty$ form
$-\frac{\infty}{\infty}$ form	$-\ 0^0$ form
	$-\ \infty^0$ form
	$- 1^\infty$ form

Chapter 5.

- Consider the integral as a measure of signed area between curve and x -axis
- Use knowledge of geometric shapes, like circles and trapezoids, to compute definite integrals
- Use basic integral rules, including:
 - $-\$ integral of a sum is the sum of the integrals
 - $-\$ integral of a constant multiple is the constant multiple of the integral
 - $-\ \int_a^b f(x)dx = \int_a^c f(x)dx + \int_c^b f(x)dx$
- Use antiderivatives to compute definite integrals and find indefinite integrals
- Use integration by substitution to solve definite and indefinite integrals
- Find the average value of a function on an interval

Chapter 6.

- Find the area between two curves
- Find the volume of a solid with a flat base and info about cross-sections
- Find the volume of a solid of revolution using either disk/washer method or cylindrical shells method
- Use integration to solve problems involving work or density
- Recall the definitions of \sinh and \cosh in terms of e^x and e^{-x} , and know their derivatives and antiderivatives

Derivatives and Integrals To Know.

- You should definitely have the following memorized:

(i) $\frac{d}{dx}(x^n) = nx^{n-1}$	$\int x^n dx = \frac{x^{n+1}}{n+1} + C$
(ii) $\frac{d}{dx}(\sin(x)) = \cos(x)$	$\int \cos(x) dx = \sin(x) + C$
(iii) $\frac{d}{dx}(\cos(x)) = -\sin(x)$	$\int \sin(x) dx = -\cos(x) + C$
(iv) $\frac{d}{dx}(e^x) = e^x$	$\int e^x dx = e^x + C$
(v) $\frac{d}{dx}(\ln(x)) = \frac{1}{x}$	$\int \frac{1}{x} dx = \ln(x) + C$
(vi) $\frac{d}{dx}(\tan^{-1}(x)) = \frac{1}{1+x^2}$	$\int \frac{1}{1+x^2} dx = \tan^{-1}(x) + C$
(vii) $\frac{d}{dx}(\sinh(x)) = \cosh(x)$	$\int \cosh(x) dx = \sinh(x) + C$
(viii) $\frac{d}{dx}(\cosh(x)) = \sinh(x)$	$\int \sinh(x) dx = \cosh(x) + C$

- Additionally, you may want to either memorize or remember the process of finding the derivatives and/or integrals of the following functions:
 $\tan(x)$, $\sec(x)$, b^x , $\log_b(x)$, $\sin^{-1}(x)$, $\cos^{-1}(x)$, $\tanh(x)$, $\operatorname{sech}(x)$.