

1. Compute $\lim_{x \rightarrow 2} \frac{x^2 - 2}{x^3 + 4x + 3}$.

2. Compute $\lim_{x \rightarrow 0} e^x$.

3. Compute $\lim_{x \rightarrow 4} \log_2(x)$.

4. Compute $\lim_{x \rightarrow 3} \frac{x^2 - 6x + 9}{x^2 - 9}$.

5. Compute $\lim_{x \rightarrow -1} \frac{\sqrt{2x+3} - 1}{x+1}$.

6. Compute $\lim_{x \rightarrow 0} \frac{(x+2)^3 - 8}{x}$.

7. Compute $\lim_{x \rightarrow 0} \left(\frac{1}{x\sqrt{x+1}} - \frac{1}{x} \right)$.

8. Compute $\lim_{x \rightarrow 0^-} \left(\frac{1}{x} - \frac{1}{|x|} \right)$.

9. Compute $\lim_{x \rightarrow 0^+} \ln(x)$.

10. Compute $\lim_{x \rightarrow 0} \frac{\sin(2x)}{x}$.

11. Compute $\lim_{x \rightarrow \infty} \frac{2x^3 - 4x + 18}{x^3 + 20x^2 + 11x + 13}$.

12. Compute $\lim_{x \rightarrow -\infty} \frac{5x^2 + 10x - 1}{x^3 + 2}$.

13. Compute $\lim_{x \rightarrow 1} \frac{x^3 - 2x^2 + 1}{x^3 - 1}.$

14. Compute $\lim_{x \rightarrow 0} \frac{e^{2x} - 1}{\sin(x)}.$

15. Compute $\lim_{x \rightarrow \infty} \frac{\ln(x)}{\sqrt{x}}.$

16. Compute $\lim_{x \rightarrow 0^+} \frac{\ln(x)}{\sqrt{x}}.$

17. Compute $\lim_{x \rightarrow -1} \frac{x^9 + 1}{x^5 + 1}.$

18. Compute $\lim_{x \rightarrow 0} \frac{\sqrt{1+2x} - \sqrt{1-4x}}{x}.$

19. Compute $\lim_{x \rightarrow 0} \frac{e^x - 1 - x}{x^2}.$

20. Compute $\lim_{x \rightarrow 0} \frac{\ln(1+x)}{\sin(x) + e^x - 1}.$

21. Compute $\lim_{x \rightarrow \infty} x^3 e^{-x^2}.$

22. Compute $\lim_{x \rightarrow 0^+} x^{\sqrt{x}}.$

23. Compute $\lim_{x \rightarrow \infty} x^{1/x}.$

24. Compute $\lim_{x \rightarrow 0^+} (1-x)^{1/x}.$

25. Use the Squeeze Theorem to find $\lim_{x \rightarrow 0} x^2 \sin(\frac{\pi}{x})$.

26. Let $f(x) = \frac{x^2 - 16}{2x^2 + 8x}$. Find any discontinuities and determine whether they are removable, jump, or infinite.

27. Let $f(x) = \frac{x^2 + 2x + 1}{x^2 - 1}$. Find any discontinuities and determine whether they are removable, jump, or infinite.

28. Let $f(x) = x^2 + 3x - 2$. Use the limit definition of the derivative to compute $f'(4)$.

29. Let $f(x) = \frac{2}{x+3}$. Use the limit definition of the derivative to compute $f'(x)$.

30. Let $f(x) = x \ln(x^2)$. Find $f'(x)$.

31. Let $f(x) = e^{-x^2}$. Find $f'(x)$.

32. Let $f(x) = \sin(x)e^{-\cos(x)}$. Find $f'(x)$.

33. Let $f(x) = \frac{6x}{\ln(x)}$. Find $f'(x)$.

34. Let $f(x) = \sqrt{\sec(x)}$. Find $f'(x)$.

35. Let $f(x) = \ln(x) \ln(\ln(x))$. Find $f'(x)$.

36. Let $f(x) = e^x e^{(e^x)}$. Find $f'(x)$.

37. Let $f(x) = \tan(e^x)e^{-x}$. Find $f'(x)$.

38. Let $f(x) = \cosh(x^2)$. Find $f'(x)$.

39. Find the equation of the line tangent to the curve $y = e^{\sin(x)}$ at the point $(0, 1)$.

40. Let $f(x) = xe^x$. Find $f''(x)$.

41. Consider the curve $x - 2y = \ln(xy)$. Find $\frac{dy}{dx}$.

42. Consider the curve $(1+x)^2y^2 = e^x$. Find the equation of the tangent line to this curve at the point $(0, -1)$.

43. Let $f(x) = \int_1^{\ln(x)} e^t dt$. Find $f'(x)$.

44. The radius of a spherical bubble is increasing at a rate of 2 mm/min. At what rate is the volume increasing at the moment when the radius is 40 mm? You may use the fact that the volume of a sphere is given by $V = \frac{4}{3}\pi r^3$.

45. Two people start from the same point. One walks east at 3 mph and the other walks south at 2 mph. How fast is the distance between the people changing after a half hour?

46. Use a linear approximation to the function $f(x) = \ln(x)$ at $a = 1$ to estimate the number $\ln(0.95)$.

47. Use a linear approximation to the function $f(x) = e^x$ at $a = 0$ to estimate the number $e^{-1/2}$.

48. Consider the function $f(x) = x^2 e^x$. Find the intervals on which f is increasing or decreasing, find the local maximum and minimum values of f , find the intervals of concavity of f , and find the inflection points of f .

49. Consider the function $f(x) = \frac{x^2 - 3x - 10}{x^2 - 4}$. Find the intervals on which f is increasing or decreasing, find the local maximum and minimum values of f , find the intervals of concavity of f , find the inflection points of f , find any vertical and horizontal asymptotes of f , and sketch the graph of f .

50. A box with a square base and an open top must have a volume of 1000 cm³. Find the dimensions of the box that minimize the amount of material used.

51. A cylindrical box must have a volume of 1000 cm³. The side of the box is to be made of a material that costs \$0.10 per cm² and the circular bases of the box are to be made of a material that costs \$0.50 per cm². Find the dimensions of the box that minimize the cost of the box. You may use the facts that the volume of a cylinder of radius r and height h is $\pi r^2 h$ and that the surface area of the side of the cylinder is $2\pi r h$.

52. Compute $\int_0^1 e^{2x} dx$.

53. Compute $\int_2^4 4 - \frac{6}{x^2} dx$.

54. Compute $\int_0^\pi \sqrt{x} - \cos(3x) dx$.

55. Compute $\int_0^1 \frac{4}{x^2 + 1} dx$.

56. Compute $\int_0^1 10^x dx$.

57. Compute $\int_0^1 \sinh(x) dx$.

58. Find $\int \frac{1}{x \ln(x) \ln(\ln(x))} dx$.

59. Find $\int \frac{x^2 - 2x + 1}{x} dx$.

60. Find $\int 1 + x^2 + \frac{1}{1 + x^2} dx$.

61. Find $\int \frac{1}{(x+3)^2} dx.$

62. Find $\int \frac{x}{(x+3)^2} dx.$

63. Find $\int \frac{(\tan^{-1}(2x))^2}{4x^2+1} dx.$

64. Find $\int (x+1)\sqrt{x-2} dx.$

65. Find $\int xe^{-x^2} dx.$

66. Find $\int \cot(x) dx.$

67. Find $\int \frac{e^x - 1}{e^x - x} dx.$

68. Find $\int \frac{1+x}{1+x^2} dx.$

69. Find $\int \sinh^2(x) \cosh(x) dx.$

70. Find the area of the region bounded by $y = \frac{1}{x}$, $y = \frac{1}{x^2}$, and $x = 2$.

71. Find the area of the region bounded by $y = \sin(x)$ and $y = e^x$ from $x = 0$ to $x = \pi/2$.

72. Find the volume of the solid whose base is the region bounded by $y = 2^x$ and $y = 1 + 2x - x^2$ and whose cross-sections perpendicular to the x -axis are squares.

73. Find the volume of the solid obtained by rotating the region in the first quadrant bounded by $y = \cos^{-1}(x)$ about the y -axis.

74. Find the volume of the solid obtained by rotation the region between $y = \ln(x)$ and the x -axis from $x = 1$ to $x = 3$ about the x -axis.

75. Find the work done in moving a box from $x = 0$ to $x = 1$ meters if the force acting on it is $F(x) = 3x^2$ N.

76. A spring with spring constant 12 kg/s^2 is stretched from its natural length of 1 m to 110 cm. Compute the work done.

77. A tank is a right circular cone with base radius 3 m and height 6 m, and it is filled with water up to depth 5 m. Compute the work required to pump the water out of the tank. Use 9800 N per m^3 as the density for water.

78. Find the mass of a one-dimensional rod that is 3 feet long (starting at $x = 0$) and has a density function of $\rho(x) = e^{x/2}$ lb/ft.

79. Find the average value of the function $f(x) = \frac{\ln(x)}{x}$ on the interval $[1, e]$.

80. Find the average value of the function $f(x) = \sec^2(x)e^{\tan(x)}$ on the interval $[0, \pi/4]$.

81. Let $f(x) = \frac{x\sqrt{x}}{e^{\sin(x)}}$. Use logarithmic differentiation to find $f'(x)$.

82. Find the equation of the tangent line to the curve $y = \frac{(x+1)^6 \tan^{-1}(x)}{\cos^{-1}(x)}$ at the point $(0, 0)$.
 (Hint: Use logarithmic differentiation.)

83. Let $f(x) = \ln(x) \left(\frac{1}{x^2}\right)$. Use logarithmic differentiation to find $f'(x)$.

84. Let $f(x) = \sin\left(\frac{x}{2}\right)^{\sin(x)}$. Use logarithmic differentiation to find the derivative, and use it to find the equation of the tangent line to the curve $y = f(x)$ at the point $(\pi, 1)$.

85. Let $f(x) = x^7 + 2x^5$. Find $(f^{-1})'(3)$.

86. You have a bowl that is a perfect half-sphere of radius 4 in. Water begins to enter the bowl at a rate of 1 in³/min. You want to find the rate at which the water level is rising when the water level is 2 in. To do so, you need to do the following steps:

- (a) First, you want a formula for the volume of water in the bowl when the water level is at a height h . But you notice that this volume happens to be the volume of the solid obtained by rotating the region bounded by the y -axis, the line $y = -4 + h$, and the curve $y = -\sqrt{16 - x^2}$ about the y -axis. Find this volume, in terms of h .
- (b) Set up a related rates problem using your volume formula from part (a) to compute the solution.