## EE 327 Signals and Systems 1 Homework 9

1. Find the z Transform of the following signals.

a. 
$$x[n] = \delta[n] + 7\delta[n-2] - 9\delta[n-3]$$

b. 
$$x[n] = \left(\frac{1}{4}\right)^{n-2} u[n-2]$$

c. 
$$x[n] = \left(\frac{1}{4}\right)^n (u[n-2] - u[n-5])$$

d. 
$$x[n] = nv[n]$$
 where  $v[n] = \left(\frac{1}{2}\right)^n u[n] + \left(-\frac{1}{2}\right)^n u[n]$ 

2. Find the inverse z Transform of the following signals.

a. 
$$X(z) = 5(1-z^{-1})(1+z^{-1})(1+10z^{-1})$$

b. 
$$X(z) = \frac{1}{\left(1 - \frac{1}{2}z^{-1}\right)\left(1 - z^{-1}\right)}$$

c. 
$$X(z) = \frac{3z^2 + 1}{\left(z - \frac{1}{4}\right)^2}$$

d. 
$$X(z) = \frac{z}{z^2 + 4z + 8}$$

3. Find the transfer function of the following difference equations.

a. 
$$y[n] + 0.5y[n-1] = 2x[n]$$

b. 
$$y[n] + 2y[n-2] = 2x[n] - x[n-1]$$

4. Find the final value of the following discrete-time signals.

a. 
$$X(z) = \frac{(z-1)(z+0.2)}{(z-0.3)(z+0.4)}$$

b. 
$$X(z) = \frac{z^3 + z + 1}{(z^2 - 0.25z + 0.1)(z - 1)}$$