## Automata Theory - Homework I

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## 1 Instructions

- 1. The homework is due on February 6, in class.
- 2. Attempt as many problems as you can. You will be given partial credit.

## 2 Problems

1. Given sets R, S and T, show that

$$R \cap (S \cup T) = (R \cap S) \cup (R \cap T)$$

(2 points)

2. Argue using Mathematical Induction

$$\sum_{i=1}^{n} i^3 = \left[\frac{(n) \cdot (n+1)}{2}\right]^2$$

(3 points)

- 3. Draw the transition diagram for a DFA accepting all strings  $x \in \{0,1\}^*$ , having 011 as a substring. (2 points)
- 4. Convert the NFA  $N = \langle Q, \Sigma, \delta, q_0, F \rangle$  to a DFA, where
  - $\bullet \ \ Q=\{p,q,r,s,t\},$
  - $\Sigma = \{0, 1\},$
  - $\bullet$   $\delta =$

	0	1
р	$\{p,q\}$	{p}
q	$\{r,s\}$	{t}
r	$\{p,r\}$	{t}
s	$\phi$	$\phi$
t	$\phi$	$\phi$

- $\bullet \ q_0=p,$
- $F = \{s, t\}$

(3 points)