

# Automata Theory - Scrimmage III

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## 1 Instructions

1. The Scrimmage will not be graded, i.e., there are no points.
2. Attempt as many problems as you can.

## 2 Problems

1. Minimize the states in the DFA depicted in the following diagram.

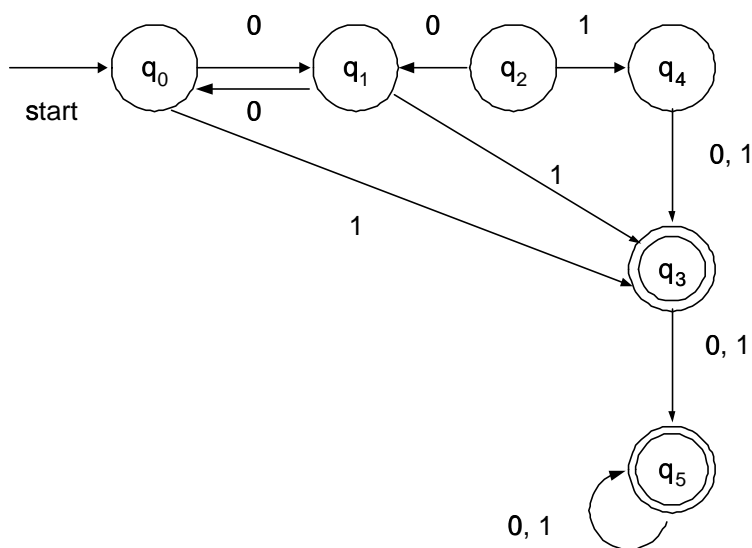


Figure 1: DFA

2. Convert the following regular expression to an NFA  $a + b^n$  where  $n \geq 1$ .
3. Convert the following  $\epsilon$ -NFA into an equivalent DFA.

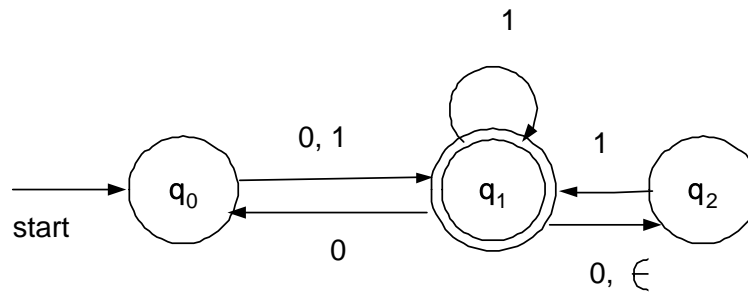


Figure 2:  $\epsilon$ -NFA

4. Give a grammar for the following language  $L = \{a^n b^m | n + m \text{ is even}\}$ .
5. Give a PDA that accepts the following language  $L = \{a^n b^n | n \geq 0\}$ .
6. Design a Turing Machine that accepts the language defined by the regular expression  $a(a + b)^*$ . Assume that  $\Sigma = \{a, b\}$ .