## Computational Complexity - Pop Quiz I

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## **1** Instructions

- (i) Attempt as many problems as you can.
- (ii) Each question is worth 1 point.

## 2 Problems

- 1. Explain with examples, the similarities and differences between
  - (a) Problems and Languages.
  - (b) Problems and Algorithms.
  - (c) Turing Machines and Algorithms.
  - (d) Recursive and Recursively enumerable languages.
- 2. Let  $L_1$  and  $L_2$  denote two recursive languages defined over the alphabet  $\Sigma = \{0, 1\}$ . Assume that  $L_1 \cap L_2 = \emptyset$ . Are  $L_1$  and  $L_2$  recursively inseparable?
- 3. State and explain Rice's theorem.
- 4. Is it possible to design an algorithm that takes as input an algorithm **A** and returns **true** if **A** correctly computes the square of its input and **false** otherwise.
- 5. Convert the following formula into CNF and DNF:

 $\bar{x_1}x_2x_3 \lor (x_1\bar{x_2} \land (x_3 \lor x_1))$