

- 7) Set up a system of equations that would allow you to determine the variables in the following flow of traffic diagram. You do **not** need to solve this system.

$$400 \rightarrow \otimes \xrightarrow{x_1} \otimes \rightarrow 350$$

$x_3 \downarrow \quad \uparrow x_4$

$$200 \rightarrow \otimes \xrightarrow{x_2} \otimes \rightarrow 250$$

$$x_1 + x_3 = 400$$

$$x_3 + 200 = x_2$$

$$x_1 + x_4 = 350$$

$$x_2 = 250 + x_4$$

$$x_1 + x_3 = 400$$

$$x_2 - x_3 = 200$$

$$x_1 + x_4 = 350$$

$$x_2 - x_4 = 250$$

8) Find the inverse of

$$\begin{bmatrix} 1 & 1 & 1 \\ 0 & 2 & 3 \\ 4 & 3 & 3 \end{bmatrix}$$

$$\left[\begin{array}{ccc|ccc} 1 & 1 & 1 & 1 & 0 & 0 \\ 0 & 2 & 3 & 0 & 1 & 0 \\ 4 & 3 & 3 & 0 & 0 & 1 \end{array} \right] \rightarrow \left[\begin{array}{ccc|ccc} 1 & 1 & 1 & 1 & 0 & 0 \\ 0 & 2 & 3 & 0 & 1 & 0 \\ 0 & -1 & -1 & -4 & 0 & 1 \end{array} \right] \rightarrow \left[\begin{array}{ccc|ccc} 1 & 1 & 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 4 & 0 & -1 \\ 0 & 2 & 3 & 0 & 1 & 0 \end{array} \right]$$

$$\rightarrow \left[\begin{array}{ccc|ccc} 1 & 0 & 0 & -3 & 0 & 1 \\ 0 & 1 & 1 & 4 & 0 & -1 \\ 0 & 0 & 1 & -8 & 1 & 2 \end{array} \right] \rightarrow \left[\begin{array}{ccc|ccc} 1 & 0 & 0 & -3 & 0 & 1 \\ 0 & 1 & 0 & 12 & -1 & -3 \\ 0 & 0 & 1 & -8 & 1 & 2 \end{array} \right]$$

$$A^{-1} = \begin{bmatrix} -3 & 0 & 1 \\ 12 & -1 & -3 \\ -8 & 1 & 2 \end{bmatrix}$$